



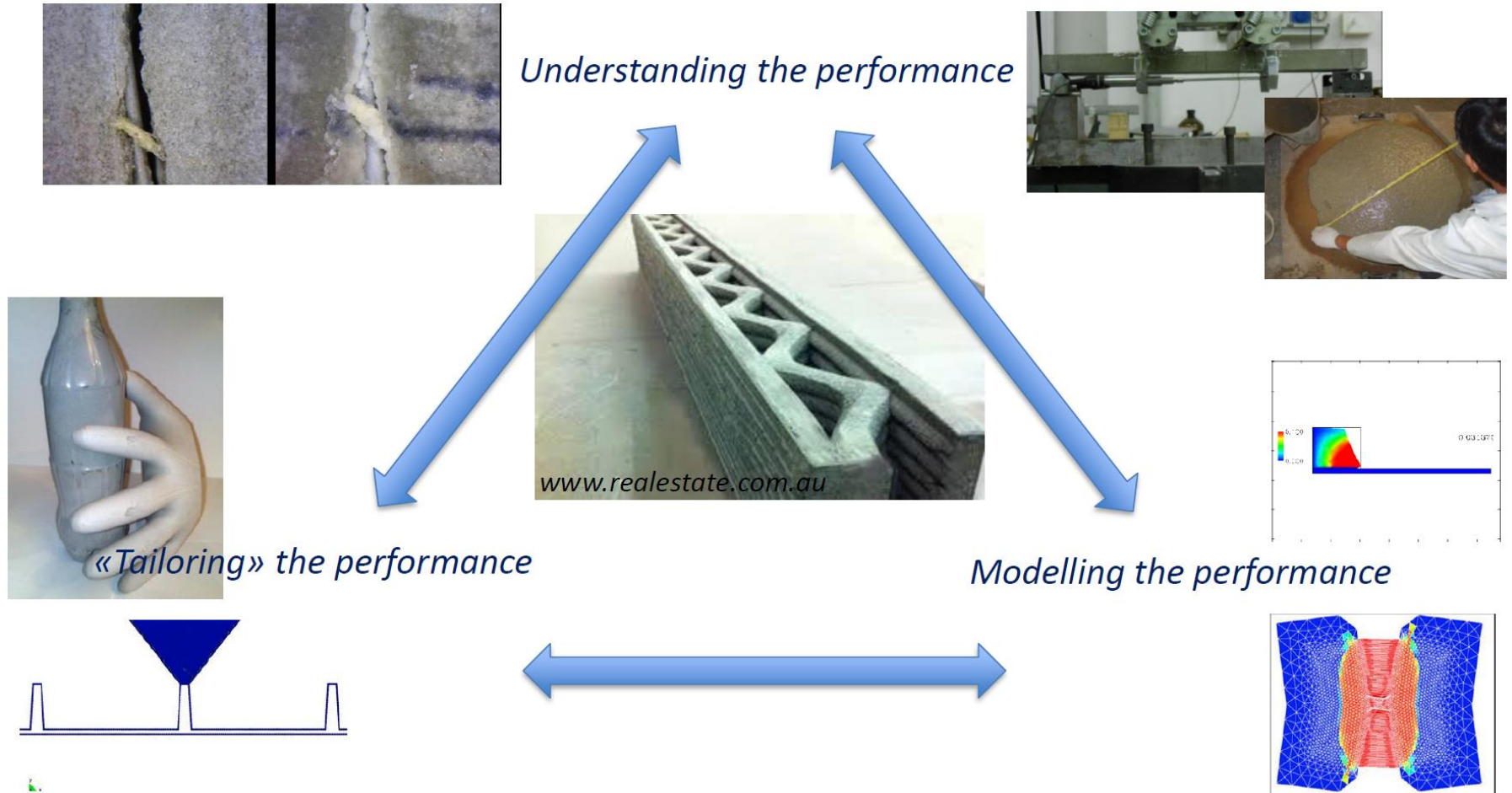
**POLITECNICO**  
MILANO 1863

# Methods for Non-Destructive Analysis of Fiber Dispersion in Fiber Reinforced Cementitious Composites

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**Department of Civil and Environmental Engineering, Politecnico di Milano**

# A holistic approach to the design of FRC structures

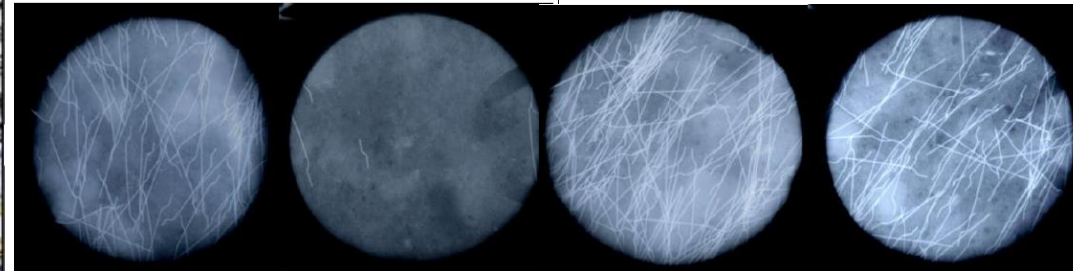




# Progresses in concrete rheology «fostering» the study of fibre orientation issues



KEY ISSUE: FIBER DISPERSION?  
Controlling the rheology!

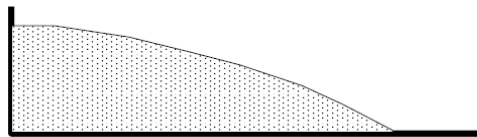


Vibrated SFRC

SCSFRC

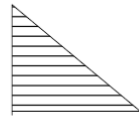
*Ferrara and Meda, Materials and Structures 2006*

# Progresses in concrete rheology «fostering» the study of fibre orientation issues



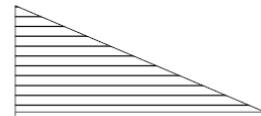
Newtonian fluid

$$\tau = 0$$



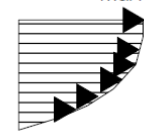
$$\tau = \tau_{max}$$

$$\dot{\gamma} = 0$$

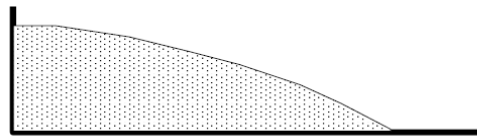
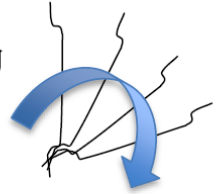


$$\dot{\gamma} = \tau_{max}/\mu$$

$$v = v_{max}$$

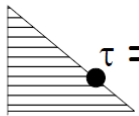


$$v = 0$$



Casting flow – NVC

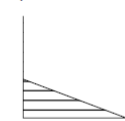
$$\tau = 0$$



$$\tau = \tau_0$$

$$\tau = \tau_{max}$$

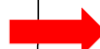
$$\dot{\gamma} = 0$$



$$\dot{\gamma} = (\tau - \tau_0)/\mu$$



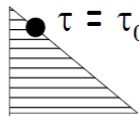
Extended plug flow  
No orientation



Bingham fluid – high  $\tau_0$

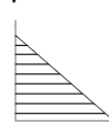
$$\tau = \tau_0 + \mu\dot{\gamma}$$

$$\tau = 0$$



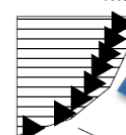
$$\tau = \tau_{max}$$

$$\dot{\gamma} = 0$$



$$\dot{\gamma} = (\tau - \tau_0)/\mu$$

$$v = v_{mc}$$



$$v = 0$$

Limited plug flow



Extended shear flow  
Orientation!

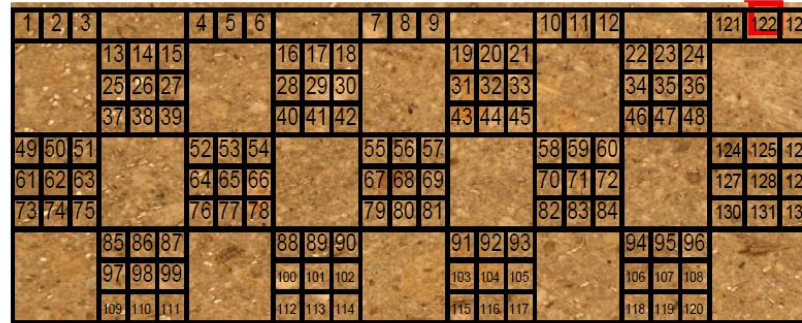
Bingham fluid – low  $\tau_0$

$$\tau = \tau_0 + \mu\dot{\gamma}$$

# Progresses in concrete rheology «fostering» the study of fibre orientation issues



Tailored casting



Micrograph analysis of mid-span section

Orientation number: projected length of fiber available along each direction

	$V_p: 0,55$	$V_p: 0,60$	$V_p: 0,65$
	$0,165$ 	$0,167$ 	$0,200$ 

*Ferrara et al., Materials and Structures, 2011*



# Monitoring the «in structure» fibre dispersion

## Control in the fresh state

“wash” and sieve the fibers

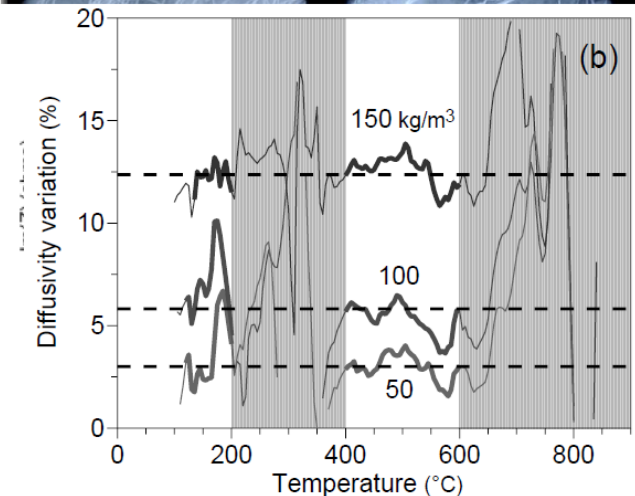
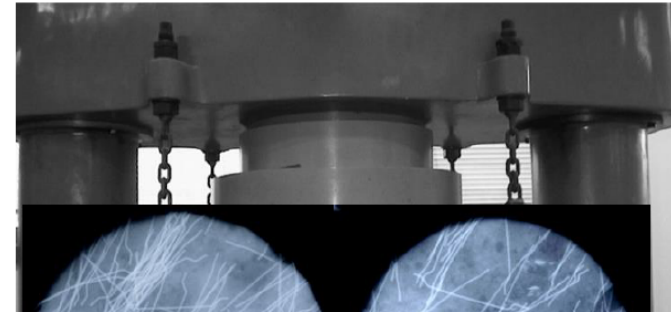
## Control in the hardened state

– Destructive methods

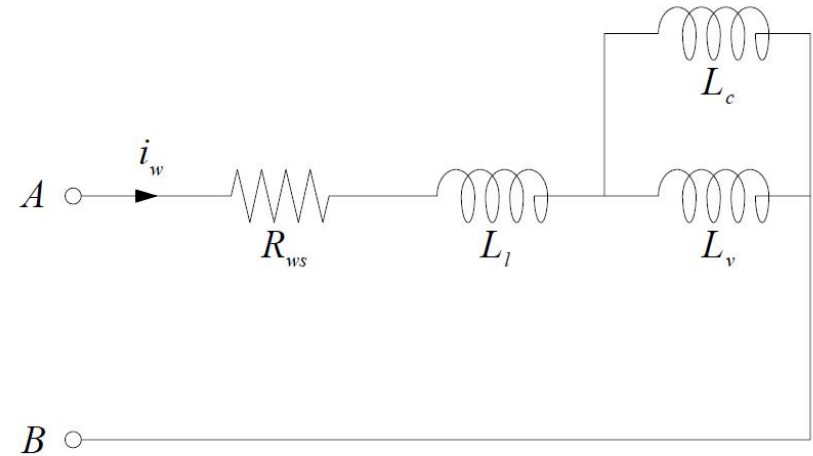
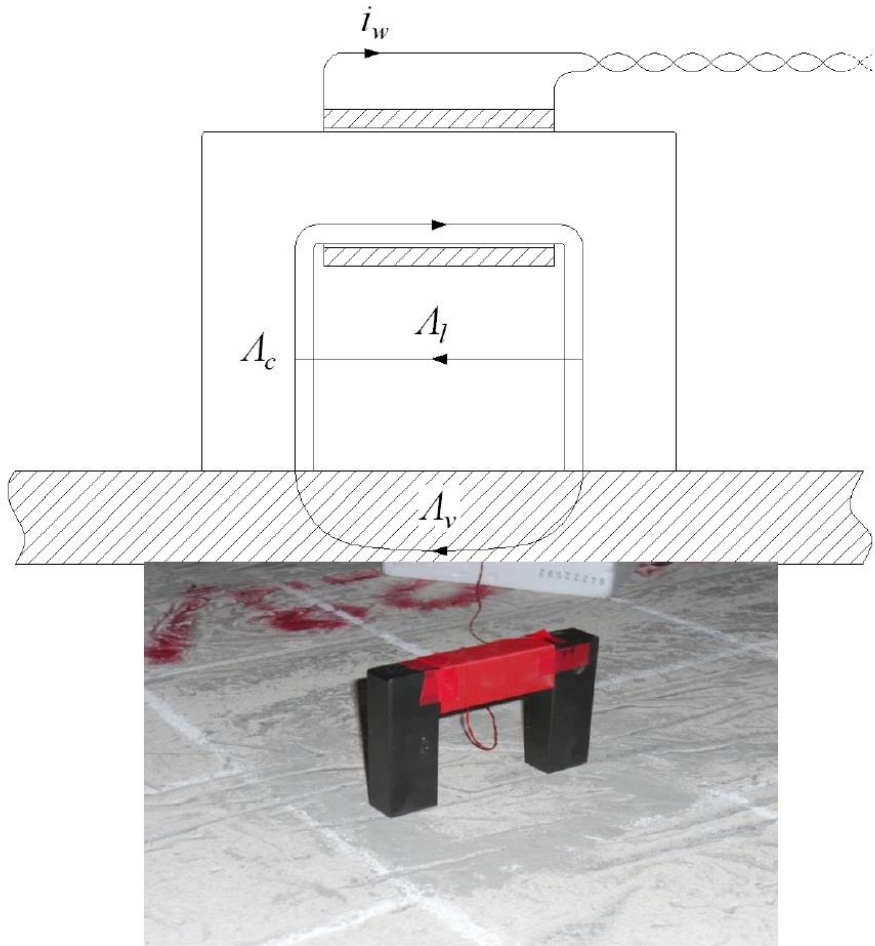
e.g.: drill cores, crush and weigh fibers

– Non-destructive methods

- X-rays
- Electrical-resistivity/impedance method  
Wansom et al., Lataste et al., Franchois
- Thermal methods (Felicetti and Ferrara)
- Magnetic inductance methods



# Monitoring the «in structure» fibre dispersion: a magnetic inductance based method



Magnetic inductance associated to the flux

$$L_v = L_{v0} + \Delta L_{\text{fibers}}$$

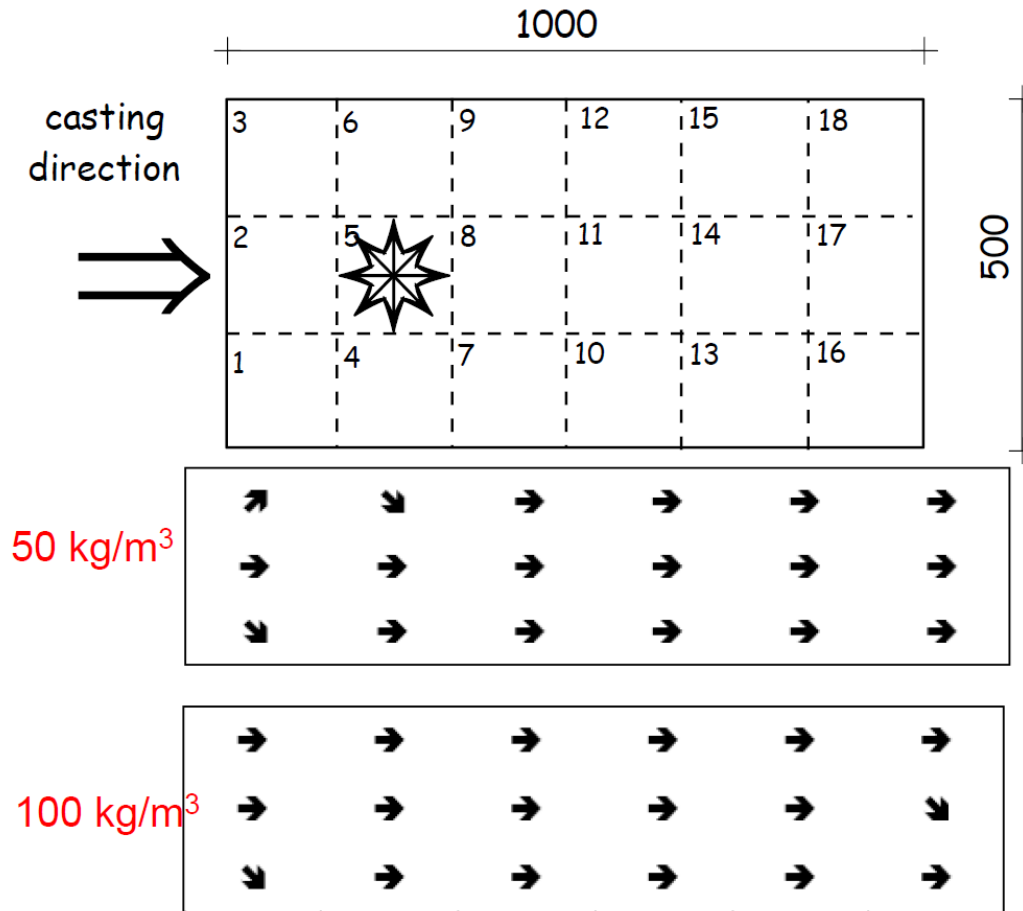
Matrix contribution  $L_{v0}$

Fiber contribution  $\Delta L_{\text{fibers}}$

Assess local concentration and orientation  
of fibers

*Ferrara et al., Materials and Structures, 2012*

# Monitoring the «in structure» fibre dispersion: a magnetic inductance based method



Per each cell:

Measures along 4 directions  
3 measures along each direction

Hypothesis confirmed:

Tailored rheology =  
flow induced fiber orientation

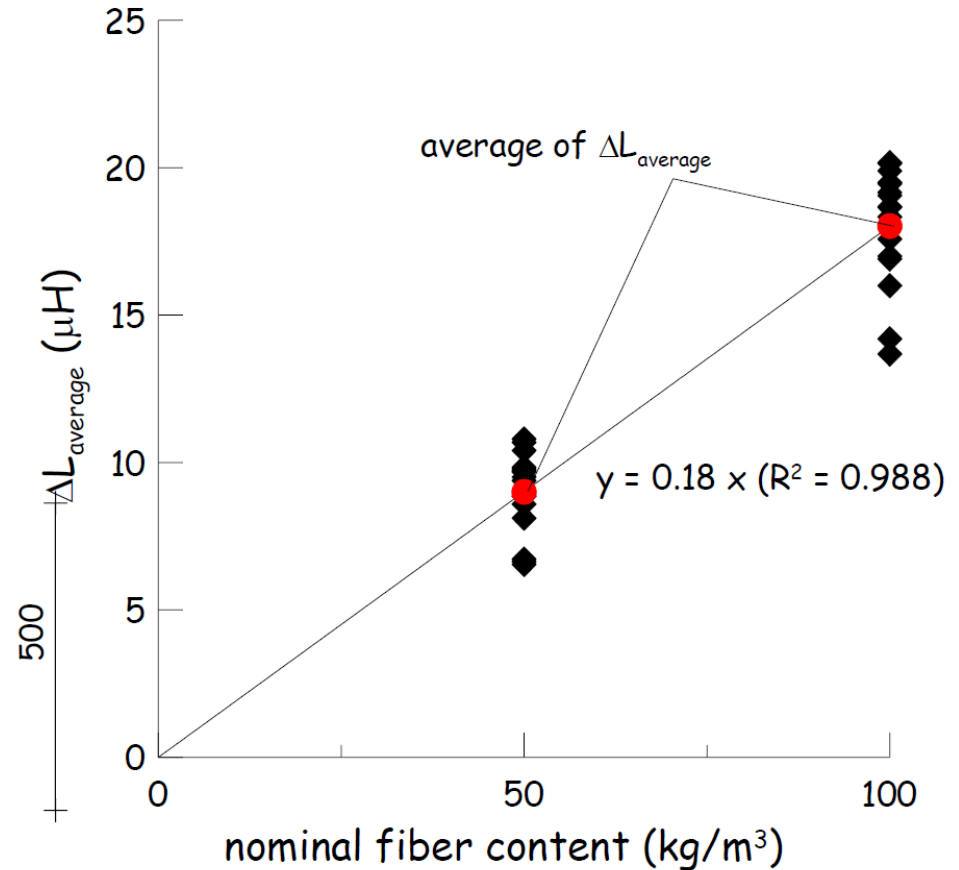
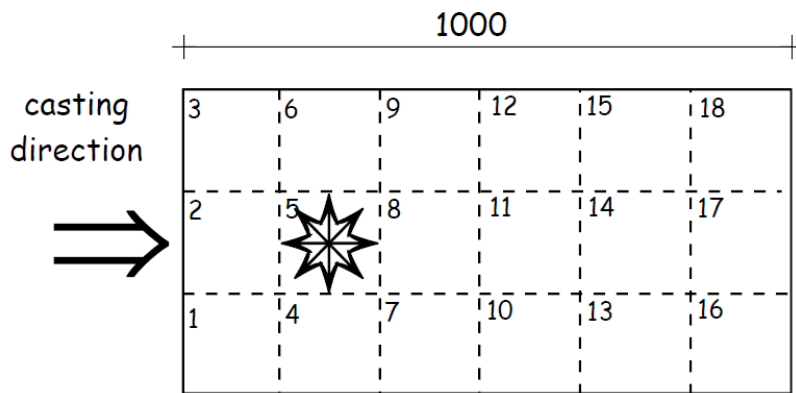
*Ferrara et al., Materials and Structures, 2012*



# Monitoring the «in structure» fibre dispersion: a magnetic inductance based method

## Calibration

Quantitative assessment of local unhomogeneities in fiber dispersion

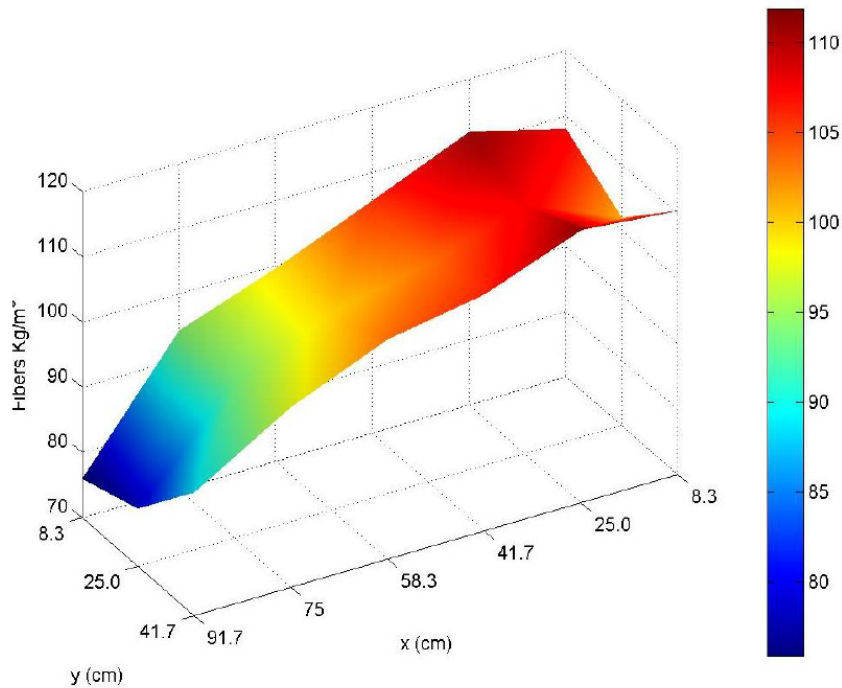


*Ferrara et al., Materials and Structures, 2012*

# Monitoring the «in structure» fibre dispersion: a magnetic inductance based method

## Calibration

Quantitative assessment of local unhomogeneities in fiber dispersion:  
check with destructive assessment

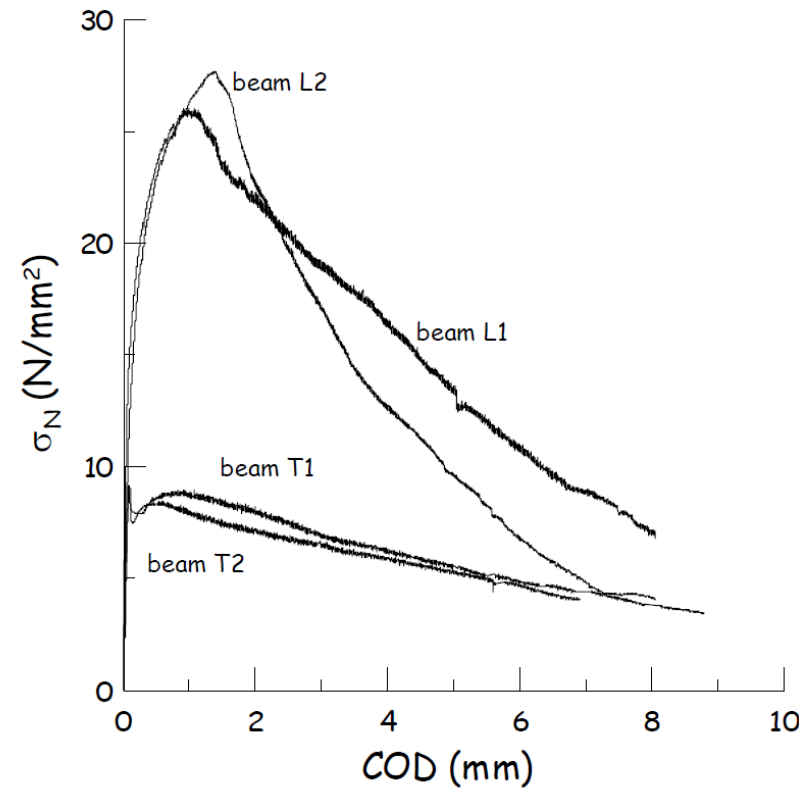
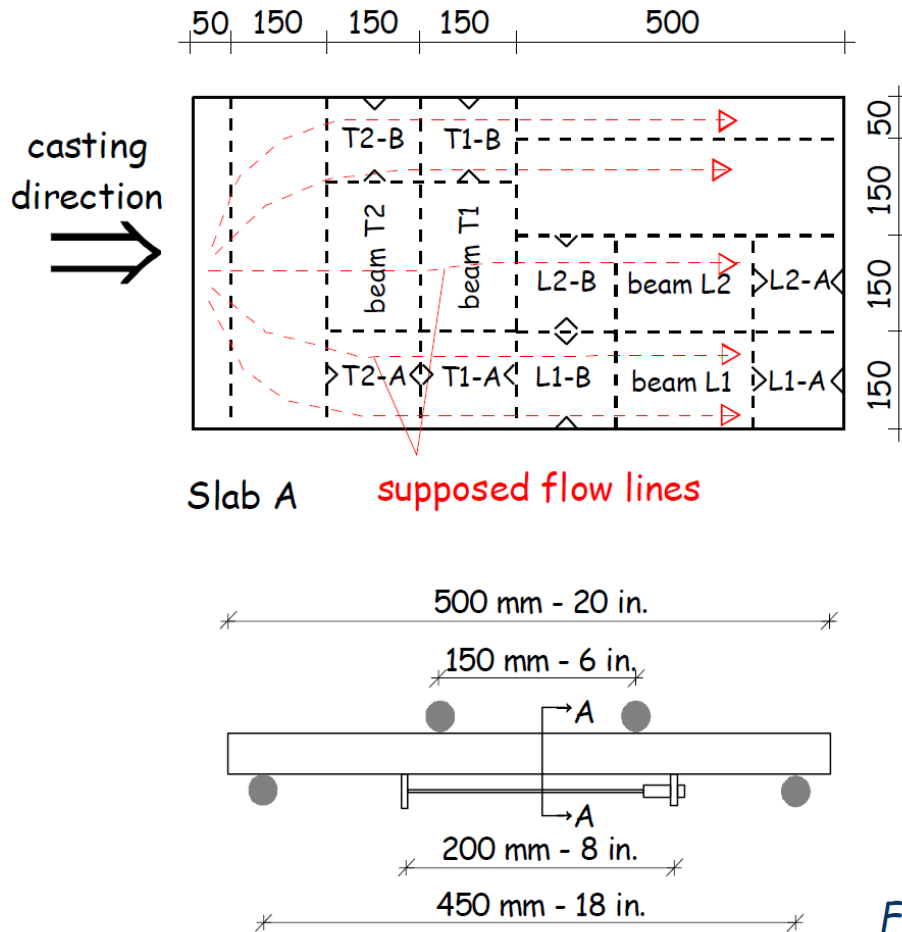


100 kg/m<sup>3</sup>

3	6	9	12	15	18
ND = 110.5	ND = 110.5	ND = 106.6 D = 109.9	ND = 103.6 D = 106.7	ND = 97.5	ND = 88.7
2	5	8	11	14	17
ND = 101.8 D = 119.1	ND = 108.7 D = 109.5	ND = 103.5 D = 107.8	ND = 100 D = 101.9	ND = 93.7 D = 98.2	ND = 79.4 D = 85
1	4	7	10	13	16
ND = 100.8	ND = 111.7	ND = 105.7 D = 105.6	ND = 99.5 D = 99.4	ND = 94.2	ND = 75.9

*Ferrara et al., Materials and Structures, 2012*

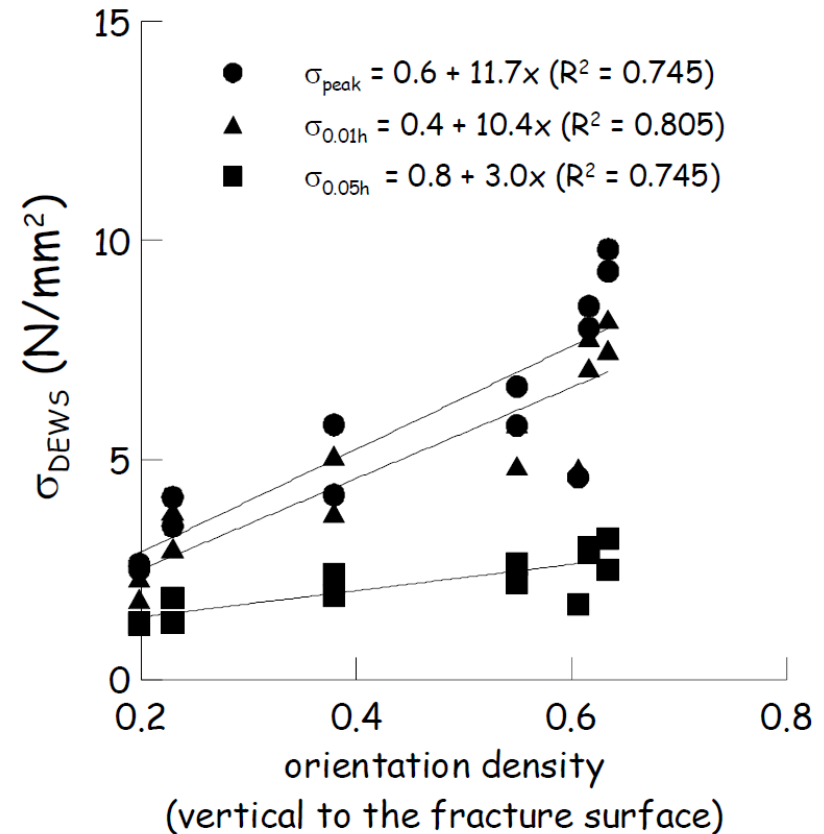
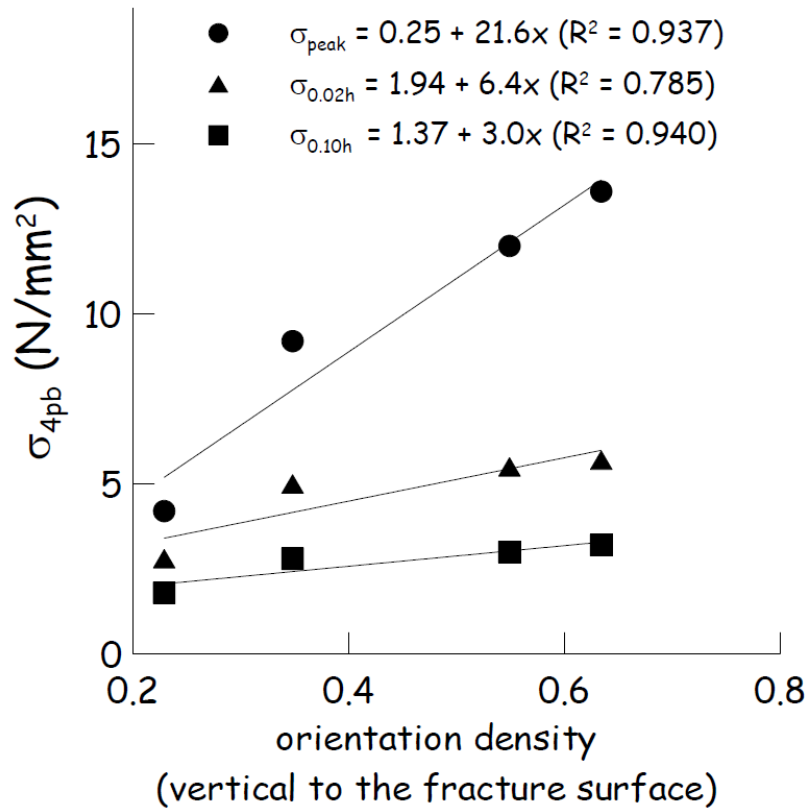
# Monitoring the «in structure» fibre dispersion: mechanical verification



*Ferrara et al., Materials and Structures, 2011*

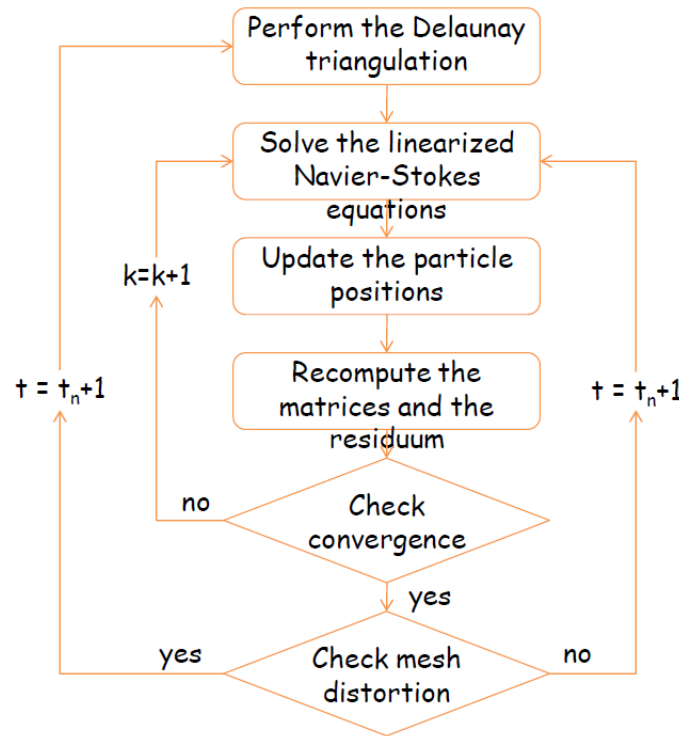
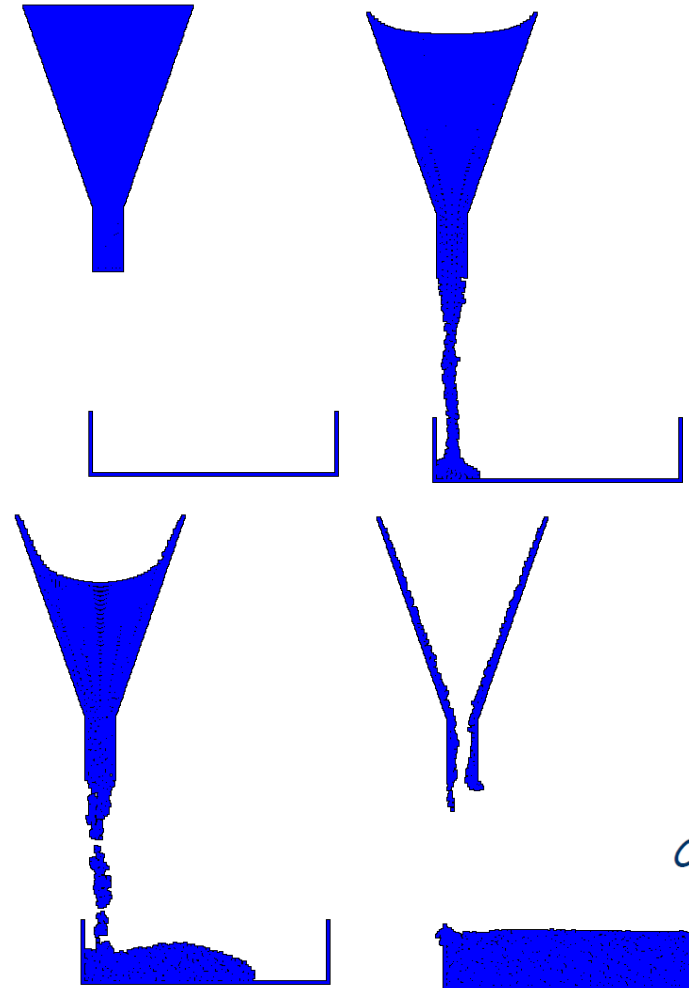


# Monitoring the «in structure» fibre dispersion: mechanical verification



*di Prisco et al., Materials and Structures, 2013*

# Predicting the «in structure» fiber dispersion: a particle finite element approach



Index of mesh distortion

for every element:

$$q_e = \sqrt{3}\alpha_e = \sqrt{3}\frac{R_e}{h_e} \gg 1$$

$h_e$  the minimal distance between two nodes in the element

$R_e$  the radius of the circumcircle

The quality of the entire mesh is then evaluated by an arithmetic mean:

$$Q = \frac{1}{N_{el}} \sum_{e=1}^{N_{el}} q_e$$

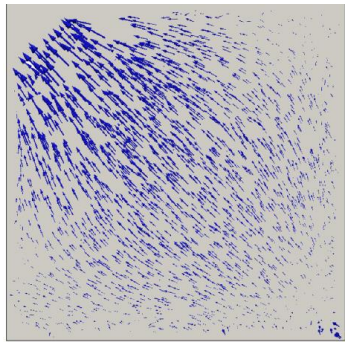
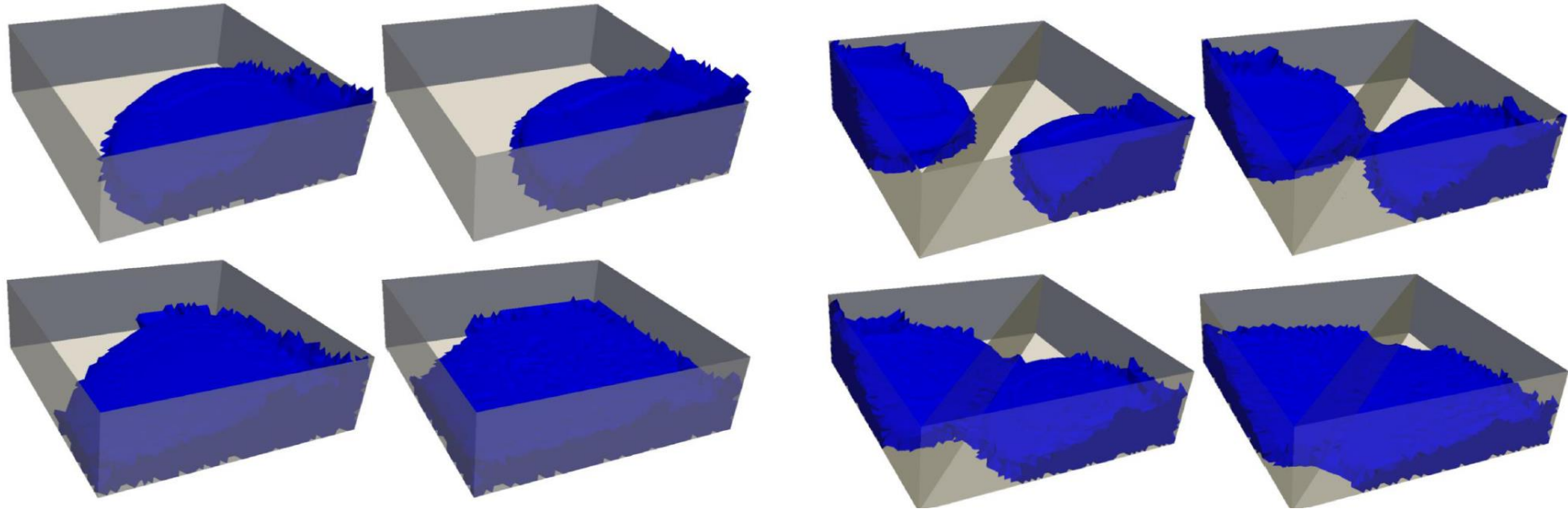
The mesh is regenerated only if:

$$Q > \beta$$

*Cremonesi et al. Journal for Numerical Methods in Engineering, 2010*

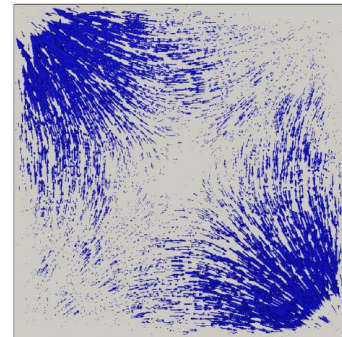
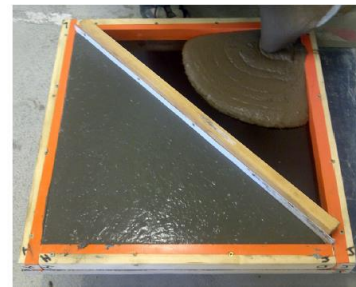
*Ferrara et al., Cement and Concrete Research, 2012*

# Predicting the «in structure» fiber dispersion: a particle finite element approach



*Sorelli et al., CBM, 2016*

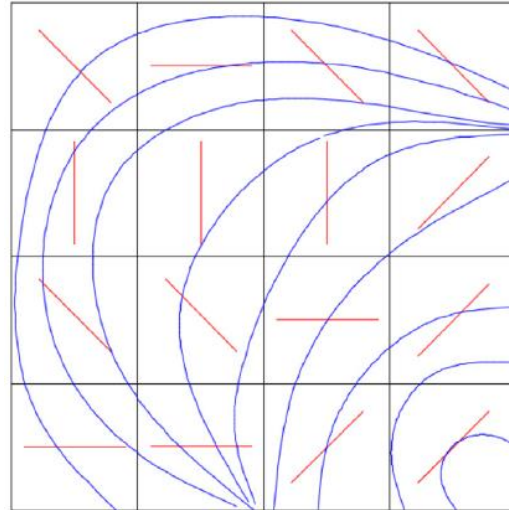
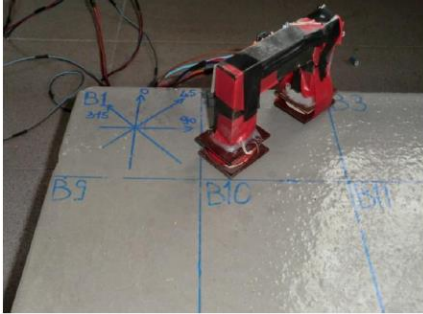
*Ferrara et al., Engineering Structures 2017*



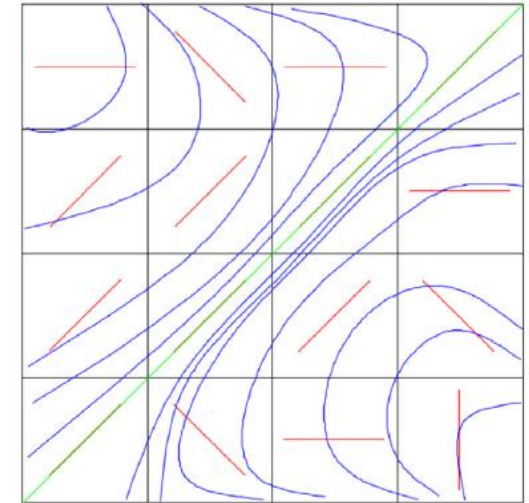


# Predicting the «in structure» fiber dispersion

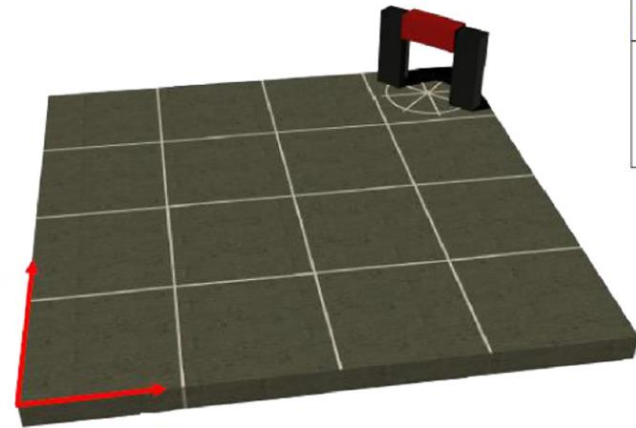
## A particle finite element approach: verification



Reference slab (1)



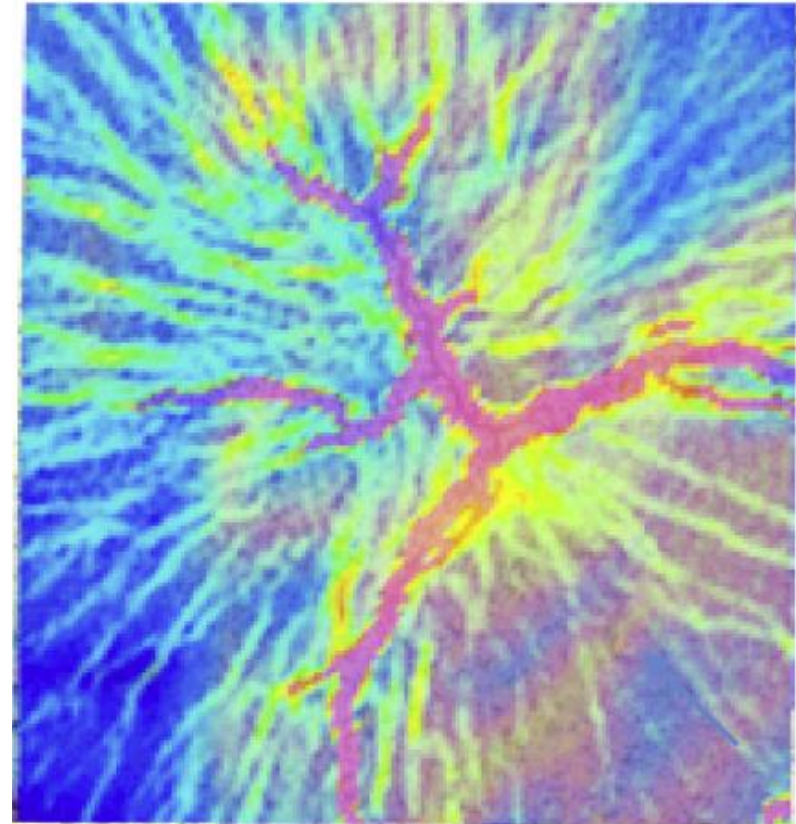
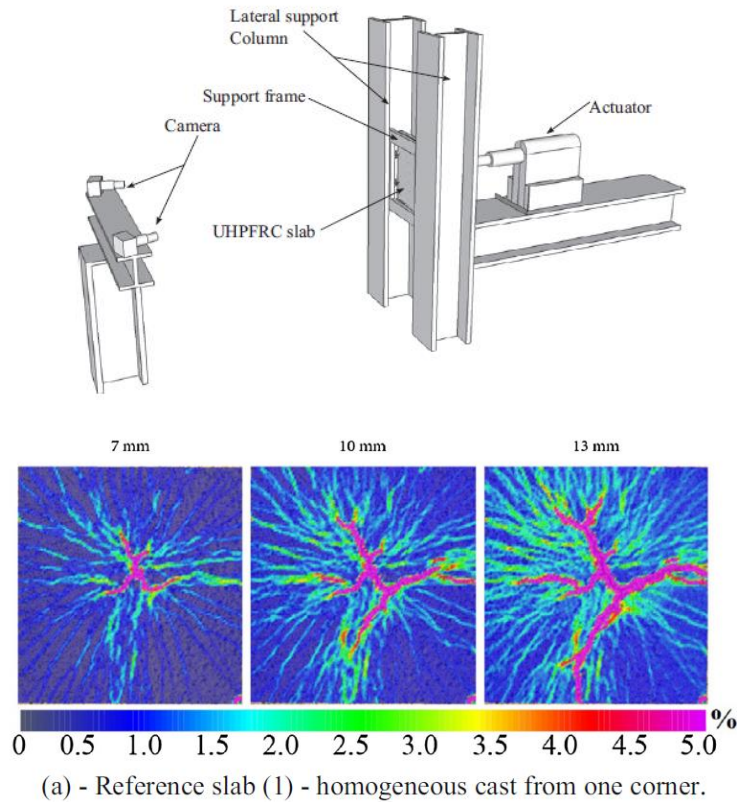
Diagonal defective cast slab (4)



*Sorelli et al., CBM, 2016*

*Ferrara et al., Engineering Structures 2017*

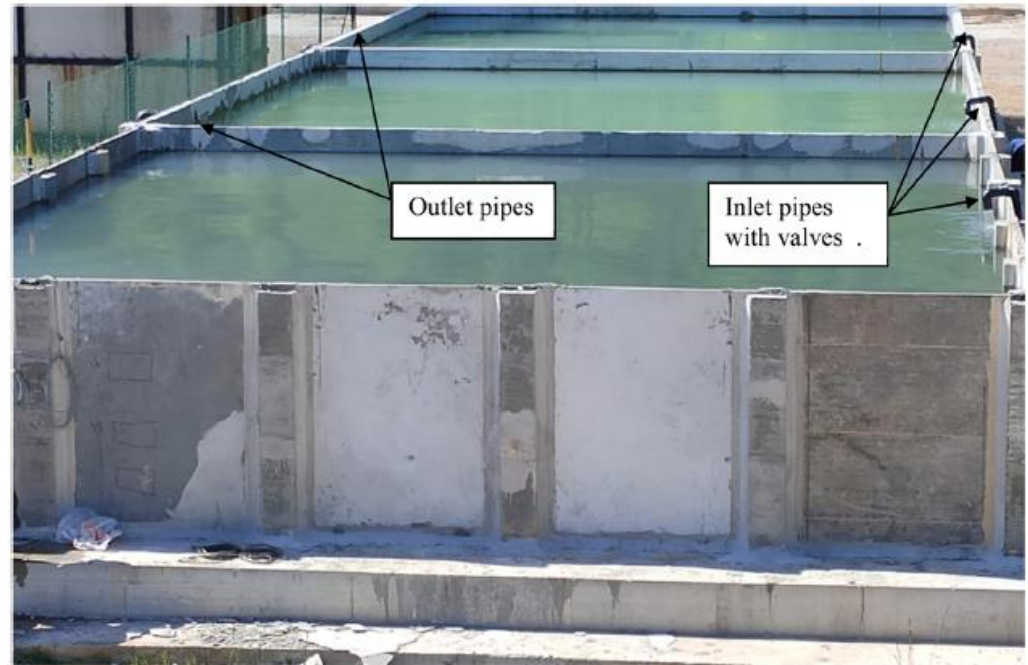
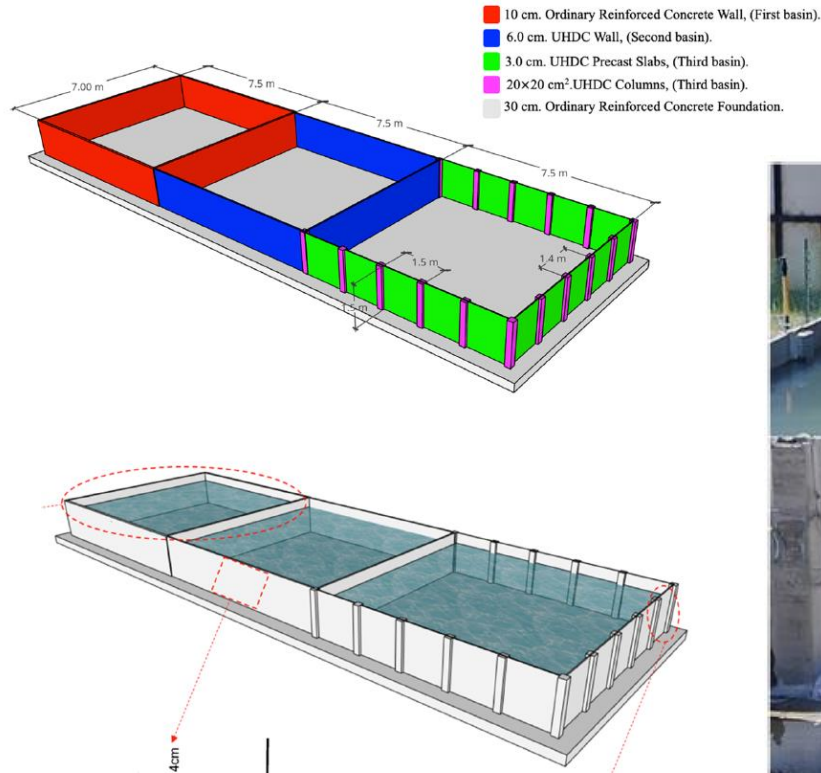
# Monitoring and predicting the «in structure» fiber dispersion: a structural check



*Sorelli et al., CBM, 2016*

*Ferrara et al., Engineering Structures 2017*

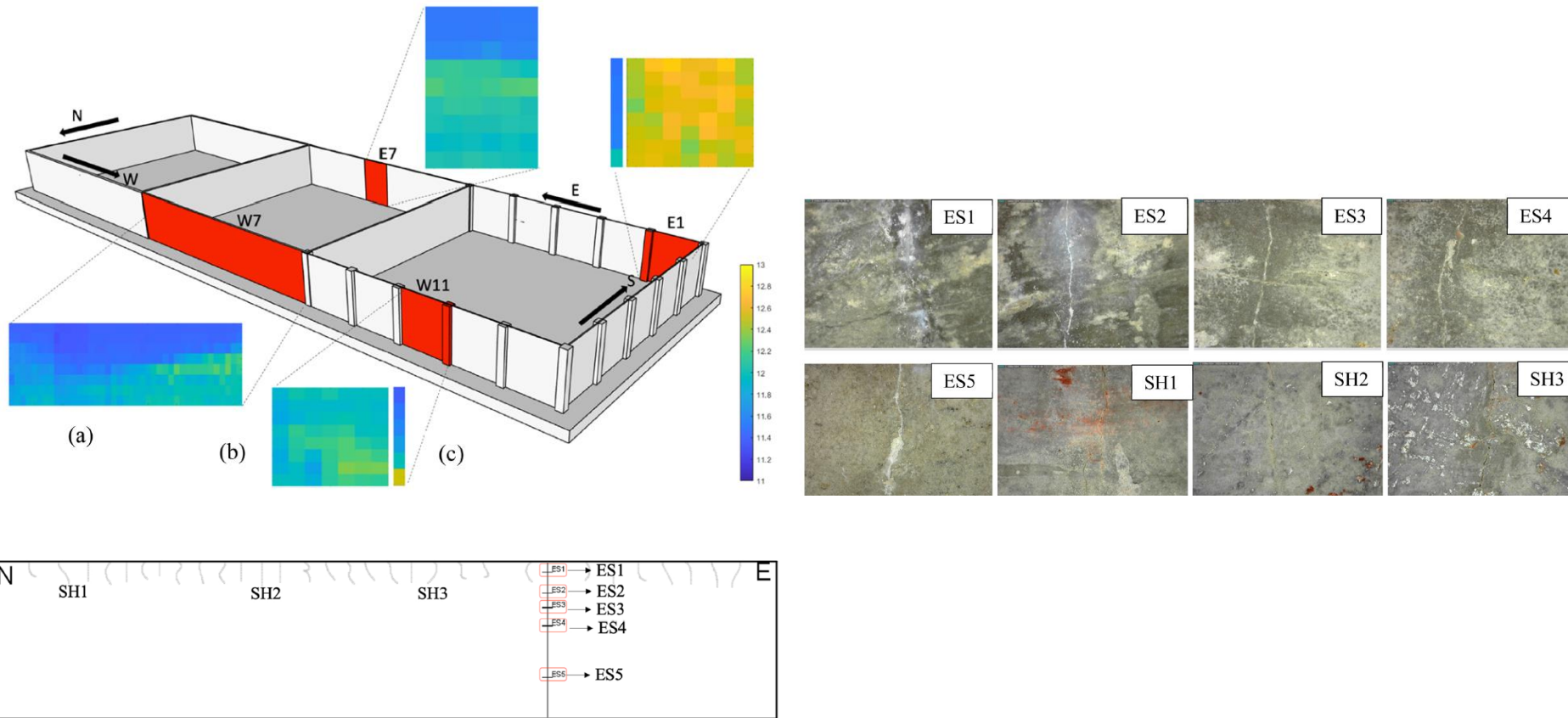
# Monitoring the «in structure» fiber dispersion: a real case study application



*Al Obaidi et al., Case Studies in Construction Materials, 2023*

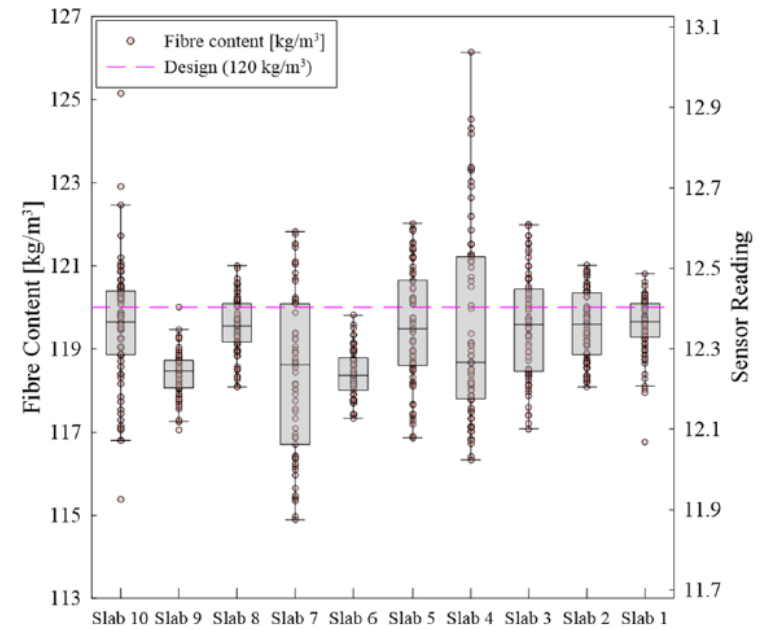
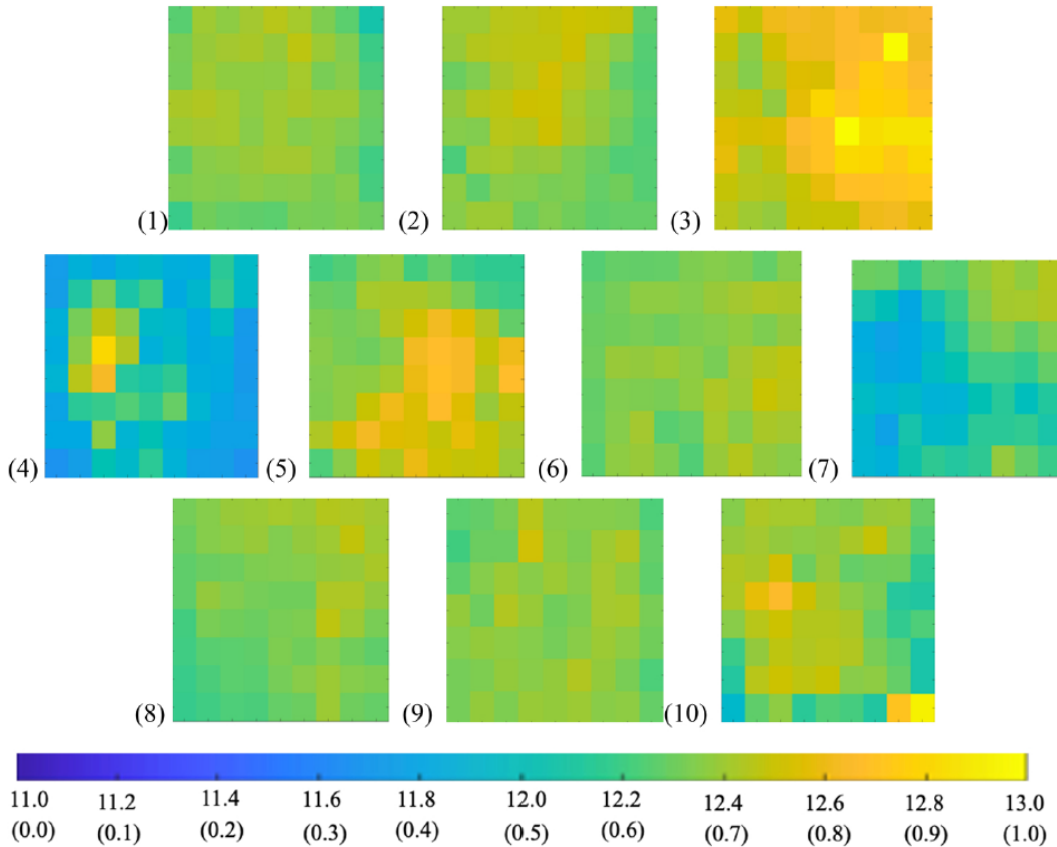


# Monitoring the «in structure» fiber dispersion: a real case study application



*Al Obaidi et al., Case Studies in Construction Materials, 2023*

# Monitoring the «in structure» fiber dispersion: a real case study application



*Al Obaidi et al., Case Studies in Construction Materials, 2023*

# Concluding remarks



Non destructive method based on magnetic inductance for fibre dispersion and orientation monitoring

Validation at the lab scale

Correlation with predictions from CFD tool and with mechanical material and structural performance

On site application to a real case study

# Thank you for your attention



*This project has been funded by the European Union – NextGenerationEU, under the National Recovery and Resilience Plan (NRRP) Mission 4 Component 2 Investment Line 1.5: Strengthening of research structures and creation of R&D “innovation ecosystems”, set up of “territorial leaders in R&D”*



*This project has received funding from the European Union's Horizon H2020 research and innovation programme under grant agreement N° 760824*